Conical Fluidized Bed with Arc Design for Improved Performance of Gas Distributor

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Abstract

Particles distributions along a conical fluidized bed were predicted by an alternative arrangement of the minimum fluidization velocity equation. The proposed approach introduces two new equations which present the particle diameter in the bed as function of: height in the bed (Z), angle of inclination of the fluidized bed wall (θ), input flow rate (Q_o), and gas distributor diameter (D_o, $2r_o$). A novel arc-shaped design of the gas distributor was suggested, which provides enhanced distribution of the gas and enables greater control on the direction of the gas inlet. The model showed that the inclination of the fluidized bed wall should not exceed a critical angle, which can be determined with the set of equations specially developed for this purpose, to prevent inhomogeneous fluidization across the bed and accumulation of particles along the walls.

By applying the Box Wilson Method, theoretical data were obtained for constant column diameter at the base (0.05 m), and varying bed height, Z, (range: 0.5 to 1.5 m), velocity of gas inlet, U, (range 0.25 to 1 m s^{-1}), and balance factor, a, (range: 0.5 to 1, a new factor), respectively. The angle of inclination of the wall was first predicted based on the above parameters, and subsequently, the particle size distribution along the column was determined. Theoretically the novel arc-shaped distributor design has shown the potential of generating homogeneous fluidization regimes along the bed.

Keywords: conical distributor design, fluidized bed, particle distribution, particle size, particle trajectory

1. Introduction

Fluidized bed (FB) has been under research for a long time, and it has been used for various industries because of the high mixing and contact surface area between the particles and the fluidization fluid, which lead to high mass and heat transfer (Janvijitsakul & Kuprianov, 2008). The variety of fluidized beds encountered in commercial operation is enormous and includes powders having mean sizes as small as 15μm and large as 6mm, bed diameters from 0.1 to 10m, bed depths from a few centimeters to 10m and gas velocities from 0.01 to 3m/s or even as high as 10m/s for recirculating high velocity beds. The behavior of particulate solid in fluidized beds depends largely on a combination of their mean particle size and density, and it has become increasingly common to discuss fluidized systems in relation to the so-called Geldart fluidization (Ihsan Hamawand, 2004, Ihsan Hamawand, 2009). The minimum fluidization velocity is very important parameter in a fluidized bed process; it depends directly to the weight of the particle, where it increases with increase in particle weight. When gas is passed upwards through a packed bed unrestrained at its upper surface, the pressure drop increases with gas velocity until, on the microscopic scale, the drag on an individual particle exceeds the force exerted by gravity or, on the macroscopic scale, the pressure drop across the bed equals the weight of the bed per unit area (Ihsan Hamawand, 2004).

One of the FB design is the conical fluidized bed, introduced in industries like combustion of biomass to produce energy (Janvijitsakul and Kuprianov, 2008; Kuprianov et al., 2006; Kuprianov et al., 2005; Permchart and Kuprianov, 2004), and agglomeration of particles in pharmaceutical application to modify their physical properties, size, shape, density and porosity (Jimenez et al., 2006; Wormsbecker et al., 2005, 2009; Chaplin et al., 2005). Conelike bunks have been connected broadly in different procedures, for example, the covering, drying and granulation of particulate materials and immobilized wastewater treatment and microorganism forms. In a cone shaped couch, where the cross area increment with the cot tallness, higher speed is kept up at the lower piece of the segment, making it conceivable to

fluidize particles of wide size disseminations. Toyohara and Kawamura (1992) demonstrated that particles in a taped gas-solids fluidized couch circled in the middle of center and the annulus area in a very nearly consummately blended state, which helped advance blending. Many of the Drying technology using conical shape FB, found that when the granule is initially very wet, the flow of fluidizing gas centralized (Pugsley et al., 2007). After this period, data shows that as the granule dried the centralized gas flow breaks apart and particle mixing improve this likely associate with higher rate of drying. The behavior of particle inside the conical FB are studied by (Wiens and Pugsley, 2006), where the dense particle region are gathered near the wall of the FB with decreasing solid concentration toward the center. For high moisture content there is a presence of centralized core bubble in the bed and more uniform fluidization through the bed cross section towards the end of the drying process (Chaplin et al., 2004).

Many literatures studied the hydrodynamic characteristics of the conical bed with three different cone angles, the results show that there are fixed bed, partially fluidized and spouting bed regime (Shan et al., 2000, 2001). The other kind of conical bed is the conical spouted bed, where it is used in pyrolysis of plastic and tire waste, it gives the same patterns of the fluidization regions (Wang et al., 2006; Olazar et al., 2006; Aguado et al., 2005; Olazar et al., 1995). In regards to the gas distributer, a flat plate distributor design is studied by (Son et al., 2006), to show its effect on the behavior of fluidization at the fully fluidized region.

The hydrodynamic characteristics in conical bed with flat plate distributor and different cone angle were studied and modeled to show their effect on the fluidization velocity (Kaewklum and Kuprianov, 2008; Biswal et al., 1985). In spite of the widely used conical fluidized bed, its hydrodynamic properties are not fully understood. In this theoretical study a conical gas distributer was applied, where its design is very depending on the angle of the conical FB. The direction of the holes in the distributor is set parallel to the FB wall inclination. Some papers studied the conical fluidized bed with conical distributor which is roughly stands for ash-agglomerating fluidized bed coal gasifier (Cao et al., 2008; Bi and Kojima, 1996; et al., 1997).

A few studies have endeavored to anticipate the base fluidization speed of both gas-robust and fluid strong decreased fluidized bunks by joining the cone shaped geometry into the base fluidization speed comparison. Zhou et al. (2009) changed for the forecast of Umf in a three-stage tapered fluidized couch by representing the geometrical variety of the cone shaped bunk. It is observed that the adjusted Tune et al. model gave a superior assention than the changed Zhang et al. model in examination with the current exploratory information. Dora et al. (2013) decided the hydrodynamic qualities of fluidization in a tapered couch incorporate the base fluidization speed, cot variance, and bunk extension degrees. The reliance of these amounts on a normal molecule measurement, mass division of the fines in the mixture, introductory static cot tallness, and cone edge is examined. Jernej et al. (2014) proposed a new histogram method for the detection of minimum velocity for a fully fluidized bed, the method is statistically oriented. The histogram method uses measured data, i.e., bed pressure drop versus fluidization velocity. The minimum velocity of full fluidization is determined as the inferior fluidization velocity of the most frequent pressure drop over the fluidized bed. With this method, occasional pressure jumps around the minimum fluidization velocity were distinguished from the pressure fluctuations. The histogram method was developed on the basis of experimental results.

The novelty of this theoretical study is the arc shaped-design of the gas distributor, this will allow a homogenous distribution of the fluidization gas across the bed (radially). This may eliminate dead or particle accumulation zones as in the case of flat plate distributor. To get such result, an accurate design for the distributor must take place with a sufficient thickness. This will allow a range of minimum fluidization velocity along the vertical axis of the fluidized bed. This will allow the dried particle at the bottom of the FB to migrate to higher level as they loss more moisture.

2. Objective

The objective of this study is to investigate the performance of a novel conical fluidized bed, which has an arc-shaped gas distributor. A theoretical model was specially developed for this case, which enables determining the critical angle of inclination of the wall and the design of the arc-shaped gas distributor. It was hypothesized that such design will allow for greater uniformity of gas distribution within the conical bed, both radially and vertically. Compared with the commonly used flat-plate distributor design, it has a potential to produce more complete fluidization within the entire bed with significantly less dead zones.

3. Theory

3.1 Hydrodynamics Theory

This theory is based on the fact that the initial velocity at the base of the conical vessel changes in the vertical direction due to the change in the bed's diameter. This provides a wide range of velocities within the vessel. At each level of the bed, the gas velocity represents a minimum fluidization velocity for a specific size range of particles. As a result, particles are distributed along the conical vessel depending on their diameters. The equation given by Wen and Yu (1966) for the calculation of minimum fluidization velocity for a range of particles' diameters is as following;

$$U_{mf} = \frac{\mu}{\rho_f d_v}\left\{(1,135.7 + 0.0408 Ar)^{1/2} - 33.7\right\} \tag{1}$$

Where:

$$Ar = \frac{\rho_g d_v^3 (\rho_p - \rho_g)g}{\mu^2} \tag{2}$$

Based on Geldart and Abrahamsen (1980), equation (1) can be used for particle diameter larger than 100 μm, groups B and D solids. For particles smaller than 100 μm in diameter, minimum fluidization is given by Baeyens' equation (Singh and Roy, 2005):

$$U_{mf} = \frac{(\rho_p - \rho_g)^{0.934} g^{0.934} d_p^{1.8}}{1,111 \mu^{0.87} \rho_g^{0.066}} \tag{3}$$

3.2 Vertical Distribution of Particles

For a conical vessel (Figure 1) with angle of inclination (θ), height (Z), bottom inlet radius (r_0), the diameter of the vessel at different heights is given by equation 4;
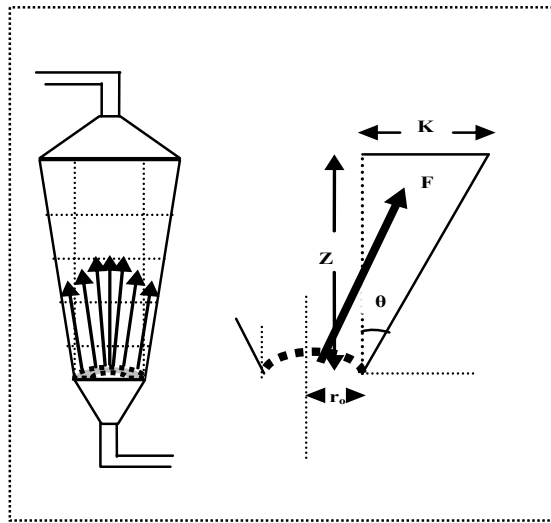
$$D_i = 2(r_o + K) \tag{4}$$

Figure 1. Description of a conical vessel and design parameters.

Where K is the increase in radius of the conical vessel with increasing height, K can be calculated from the following equations:

$$\tan\theta = \frac{K}{Z} \tag{5}$$

And,

$$K = Z\tan\theta \tag{6}$$

By substituting equation (5) in (4), the variable diameter of the vessel can be calculated as below:

$$D_i = 2(r_0 + Z\tan\theta) \tag{7}$$

Given, $C_1 = \dfrac{\left(\rho_p - \rho_g\right)^{0.934} g^{0.934}}{1{,}111 \mu^{0.87} \rho_g^{0.066}}$ and substituting it in Equation (3),

The particles' diameters can be presented as dependent variable as in equation 8;

$$d_{pi} = \left[\frac{U_{mf}}{C_1}\right]^{1/1.8} \tag{8}$$

The system of equations given below (9 and 10) and (11 and 12) describe the mass flow between two points in the conical vessel (Figure 2), namely, the entrance with diameter D_o, and any point along the column where diameter is D_i;
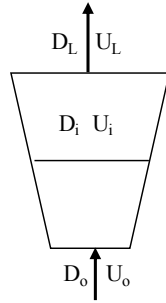
Figure 2. Graphical representation of the mass balance.

$$\rho_o U_o \frac{\pi}{4} D_o^{\,2} = \rho_i U_i \frac{\pi}{4} D_i^{\,2} \tag{9}$$

When:

$$\rho_0 = \rho_i \tag{10}$$

Also,

$$U_i = \frac{4\pi D_o^{\,2}}{4\pi D_i^{\,2}} \times U_o = \frac{4Q_o}{\pi D_i^{\,2}} \tag{11}$$

Where:

$$Q_o = \frac{\pi}{4} D_o^{\,2} U_o \tag{12}$$

Since gas velocity changes in the vertical direction according to the change in the cross sectional area of the conical vessel, then at any given height (Z), the minimum fluidization velocity is determined for specific particle diameters and specific fluidization velocity ($U_i = U_{mf}$) by equation 11. Substitution of equation (11) in equation (8) yields:

$$d_{pi} = \left[\frac{4Q_o}{\pi C_1 D_i^{\,2}}\right]^{1/1.8} \tag{13}$$

Also, substitution of equation (7) in (13) yields:

$$d_{pi} = \left[\frac{Q_o}{\pi C_1 (r_o + Z \tan \theta)^2} \right]^{1/1.8} \qquad (14)$$

Equation (14) provides material particle diameter as a function of the location of the particle (height) in the bed and the angle of inclination of the FB wall, for particle sizes smaller than 100 μm.

For spherical or near-spherical materials (sphericity ≥0.8), d_v is given by equation (15), as follows:

$$d_v = 1.13 d_{pi} \qquad (15)$$

Now for particle size greater than 100 μm, by substituting equation (15) in (1) and solving for d_{pi}, it results in:

$$d_{pi} = \frac{\mu}{1.13 \rho_g U_{mf}} \left\{ (1{,}135.7 + 0.0408 Ar)^{1/2} - 33.7 \right\} \qquad (16)$$

Also, substitute equation (11) in (16), gives:

$$d_{pi} = \frac{\pi \mu D_i^2}{4.52 \rho_g Q_o} \left\{ (1{,}135.7 + 0.0408 Ar)^{1/2} - 33.7 \right\} \qquad (17)$$

Given,

$$C_2 = \frac{\rho_g (1.13)^3 (\rho_p - \rho_g) g}{\mu^2} \qquad (18)$$

Now, subsequently, substitute equations (2), (7) and (18) in (17), yields:

$$d_{pi} = \frac{4 \pi \mu (r_o + Z \tan \theta)^2}{4.52 \rho_g Q_o} \left\{ (1{,}135.7 + 0.0408 \times (C_2)^3 (d_{pi})^3)^{1/2} - 33.7 \right\} \qquad (19)$$

Equation (19) provides the solution for particles with diameters greater than 100 μm. A convenient method to solve this equation is by trial and error since the independent variable (d_{pi}) cannot be isolated.

The gas flow rate (Q_o) must be approximately equivalent to the minimum fluidization velocity for the largest particle diameter present in the solid mixture to avoid accumulation of particles at the bottom of the bed. Due to the conical section, bed diameter increases from the bottom to the top of the bed and therefore the velocity of the gas inlet decreases accordingly. At each point along the conical vessel, this velocity represents a minimum fluidization velocity for a given particle diameter. The particles move upward as they dry and lose weight. An important practical consideration for the distributor's design is that the thickness of the wall should be sufficient to provide the required direction to the fluid inlet.

3.3 Angle of Inclination

Based on a force balance applied on a single particle, as shown in Figure 3, and in order to enable the particles to remain away from the walls and avoid dead zones in the conical vessel, it is required for the force in the horizontal direction is less than the force in the vertical direction ($F \sin \theta < F \cos \theta$).
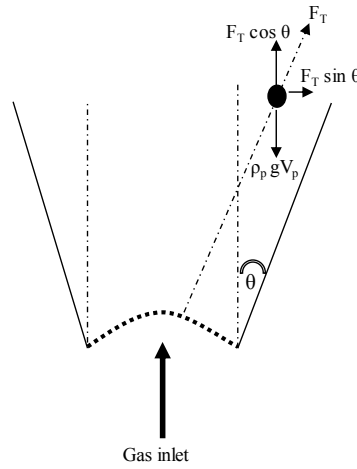
Figure 3. Graphical representation of the force balance.

The equations for the bouncy and the drag forces on a single particle are as following;

$$F_B = \frac{\pi}{6} \rho_g g d_{pi}^3 \tag{20}$$

$$F_D = \frac{\pi}{8} C_D \rho_g d_{pi}^2 U_g^2 \tag{21}$$

Where U_g is the relative velocity between the gas and the particle. Therefore, the total force balance on a single particle is as follows:

$$F_T = F_B + F_D = \frac{\pi}{24} \rho_g d_{pi}^3 \left[4g + 3C_D \frac{U_g^2}{d_{pi}} \right] \tag{22}$$

The force exerted on the particle by the gas is a combination of two components, the vertical force (gravity);

$$F_T \cos\theta = \rho_p g V_p = \frac{\pi}{6} \rho_p g d_{pi}^3 \tag{23}$$

And the horizontal force;

$$F_T \sin\theta = \frac{\pi}{24} \rho_g d_{pi}^3 \left[4g + 3C_D \frac{U_g^2}{d_{pi}} \right] \sin\theta \tag{24}$$

Let assume a new variable (a), where: $0 \le a \le 1$, which is defined as below;

$$a = \frac{F_T \sin\theta}{F_T \cos\theta - \frac{\pi}{6} \rho_p g d_{pi}^3} \tag{25}$$

Then solve equation 25 for the horizontal component;

$$F_T a \cos\theta = \frac{\pi}{6} a \rho_p g d_{pi}^3 + F_T \sin\theta \tag{26}$$

To enable for fluidization to take place, and at the same time it vector force in the vertical direction to be higher than that in the horizontal direction, the velocity of the gas at the inlet for a such particle size at such height most be larger than the minimum fluidization velocity. Substitute equation 24 in equation 26 and solve for ($a\cos\theta - \sin\theta$);

$$[a\cos\theta - \sin\theta] = \frac{\left[\dfrac{4a\rho_p g}{\rho_g}\right]}{\left[4g + 3C_D \dfrac{U_o^2}{d_{pi}}\right]} \tag{27}$$

Where d_{pi} is given by equation 14:

$$d_{pi} = \left[\frac{\dfrac{\pi}{4}D_o^2 U_o}{\pi C_1 (r_o + Z\tan\theta)^2}\right]^{1/1.8} \tag{14}$$

Equation (27) can be solved by trial and error to obtain the suitable wall angle (θ) for particles diameters smaller than 100 μm, where Z is the height of the conical vessel and 'a' can be assumed to be between 0 and 1. By applying equations (19) and (27), the solution can be obtained for particle diameters larger than 100 μm, which needs to be done by trial and error for both d_{pi} and θ. The angle of the wall in the conical vessel will therefore be between 0° and 45°.

3.4 Boundary Conditions for the Angle

When $a = 1$, then $\theta = 45°$; therefore:

$$F_T \cos\theta - \frac{\pi}{6}\rho_p g d_{pi}^3 = F_T \sin\theta$$

When $a = 0$, the shape of the column is cylindrical; therefore:

$F_T \sin\theta = 0$, and $\theta = 0°$,

When $a = 1$, and $\theta = 0°$; therefore:

$$F_T \cos\theta - \frac{\pi}{6}\rho_p g d_{pi}^3 = 0$$

4. Design of Distributor

The proposed distributor in Figure 4 consists of an arc which its design is dependent on the bottom radius of the conical vessel and the angle of inclination of the column wall. The thickness of the distributor's wall needs to be sufficient to provide the required direction to the gas through the column.
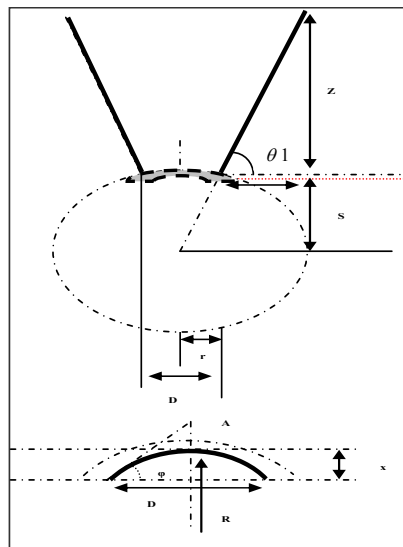

Figure 4. Specifications for the design of the proposed arc-shaped distributor.

For a fixed radius of the conical vessel and height, the angle of inclination can be obtained from equation (27). The radius of the distributor is given by equation (28), and the length of the arc is given by equation (29).

$$R = \frac{r}{\sin\theta} \qquad (28)$$

$$A = R \times 2\theta \qquad (29)$$

The other two important design parameters are the height of the arc-shaped distributor determined at the center of the conical vessel and the angle of the tangent at the end point, which can be obtained by solving equations (28) and (29), respectively.

$$x = R - \frac{D}{2\tan\theta} \qquad (28)$$

$$\varphi = \tan^{-1}\left(\frac{2x}{D}\right) \qquad (29)$$

The system of equations given above (26 to 29) will enable for optimum determination of design parameters and it confirms the importance of the angle of inclination of the wall in optimizing such design.

5. Results and Discussions

Particle diameters and balance factor were obtained by solving Equations (14) and (25), respectively. The angle of the conical fluidized bed was obtained by means of trial and error for fixed values of gas inlet velocities, base diameter of conical vessel, column height and balance factor. Subsequently, the angle thereby obtained was used for calculation of particle diameter's gradient along the bed. The angle of the wall represents the optimum angle at which full fluidization over the entire conical vessel occurs. Figures 5(a and b) shows the relationship between the relative position of particles in the conical vessel in relation to their diameter depending on the angle of the wall (θ) for fixed values of the balance factor (a =0.61 and 0.89) and gas velocity (U =0.41 and 0.84 m s^{-1}). As a result, the required height (Z) changes from 0.7 m in the former to 1.3 m in the latter. In addition, it can be seen that increase the height of the bed allows for greater angle of inclination; for example, for a =0.61 and U =0.84 m s^{-1}, θ values are 0.1 rad for Z =0.7 m and 0.18 rad for Z =1.3 m, which is explained by the space generated at higher angles enabling for more uniform particle distribution in the conical vessel. Particle distribution uniformity is at its optimum when the angle of inclination is between 0.33 and 0.37 rad, and the velocity of the gas inlet is between 0.84 and 1.0 m s^{-1}. This result is explained by the increase in the upward force due to higher velocity of the gas enabling for uniform velocity gradient within the column in the vertical direction. Figure 6 shows that an increase in the balance factor from 0.5 to 1.0 results in increased angle of inclination (from θ =0.05 rad to θ =0.16 rad, respectively) when U is maintained constant at 0.63 m s^{-1}. This means that with higher vertical force exerted on the particle, which is the situation with balance factor of 0.5, the column needs to approach a cylindrical shape (constant diameter). As the balance factor approaches a maximum value of 1.0, the force exerted on the particle in the vertical direction equates the horizontal force, which still produces a homogenous fluidization. As can be seen in figure 5(a and b), when the bed wall angle is around 0.2 and 0.37 rad there is a better distribution of the different size particles along the bed. This is due to the creation of different fluidization velocities along the bed. Higher diameter particles fluidize close to the bottom of the bed due to higher gas velocity (smaller bed diameter) and smaller diameter particles fluidize close to the top of the bed due to lower gas velocity (larger bed diameter). Similar trend in figure 6, as the bed wall angle increases, there is a better distribution of the particles along the bed.
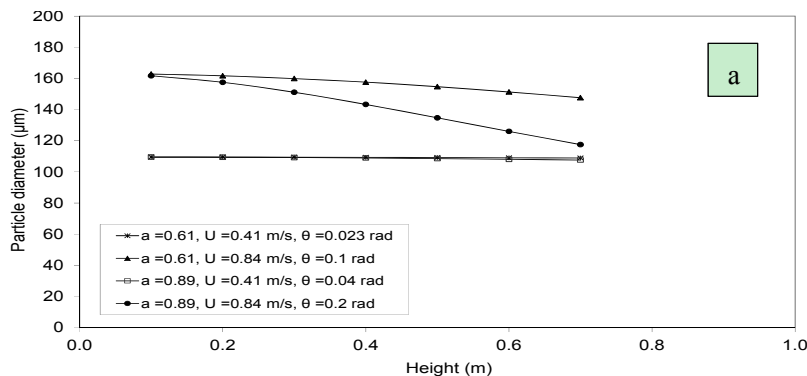
Figure 5 (a). Relationship between the relative positions of particles in the conical vessel with their diameter.
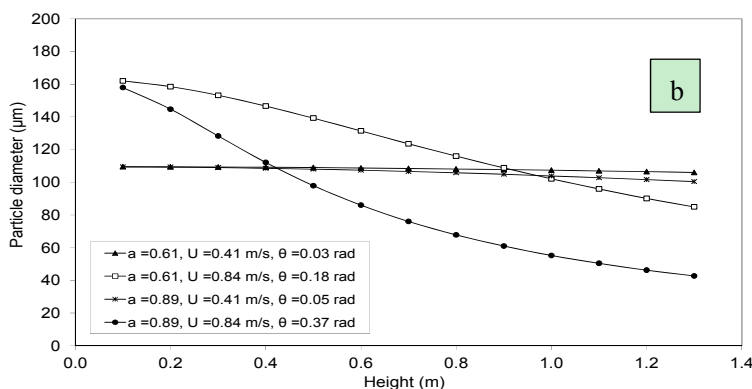

Figure 5 (b). Relationship between the relative positions of particles in the conical vessel with their diameter.
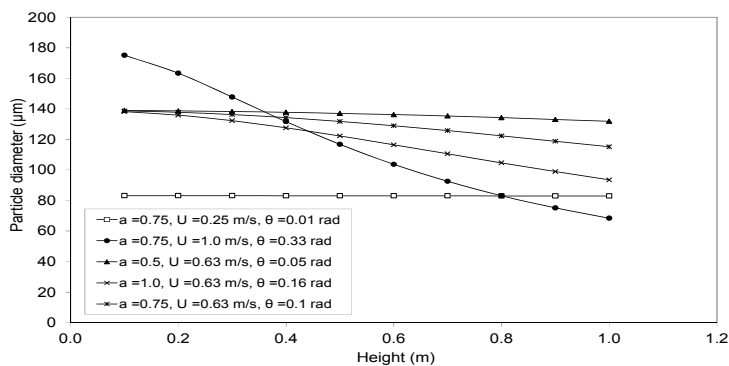

Figure 6. Relationship between the relative positions of particles in the conical vessel with their diameter.

Figures 7 to 9 were produced for a constant value of the balance factor (a) to examine the influence of gas velocity and bed height on the design of the conical bed. Figure 7 shows that there is little effect of bed height on angle of inclination (θ) since an increase in bed height from 0.7 to 1.3 m required an increase in θ from 0.023 to 0.03 rad. For the same increase in bed height but for using a gas inlet velocity of 0.84 m s^{-1}, the effect of bed height is more pronounced, which requires an increase in θ from 0.1 to 0.18, respectively. Providing the inlet gas velocity is sufficiently high to produce a homogenous fluidization, this response can be explained by the fact that an increase in bed height provides larger space and therefore enables for better particle distribution within the conical vessel. Figure 8 shows that a balance factor of 0.75, which is a reasonable value of 'a' to ensure particles remain away from the wall of the conical vessel, produces relatively poor particle distribution along the bed, except when velocity 1 m s^{-1} or higher. This observation confirms that gas inlet velocity is the main factor influencing the degree of inclination of the bed walls. The trends in both figures 7 and 8 that show better distribution of the particles are those which compensate higher bed (above 1 m), higher velocity (above 1 m/s) and higher angle of inclination (above 0.18 rad). It is obvious that higher angle of inclination of the bed walls can create a better distribution of the particles. But this happens only at sufficient height of the bed and gas inlet velocity. These variables have an interaction relationship where the balance factor is balancing the values of these
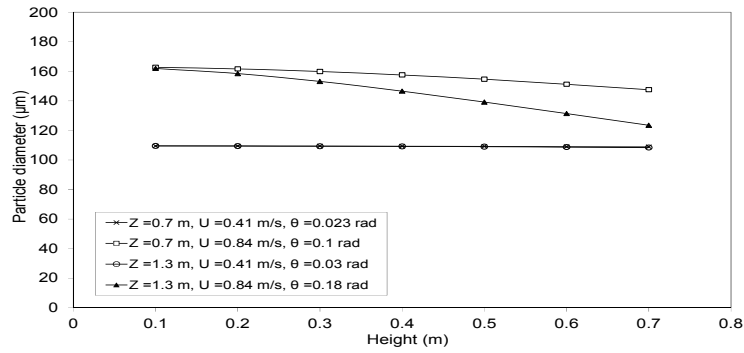
variables.

Figure 7. The influence of gas velocity and bed height on the design of the conical bed, a=0.61.
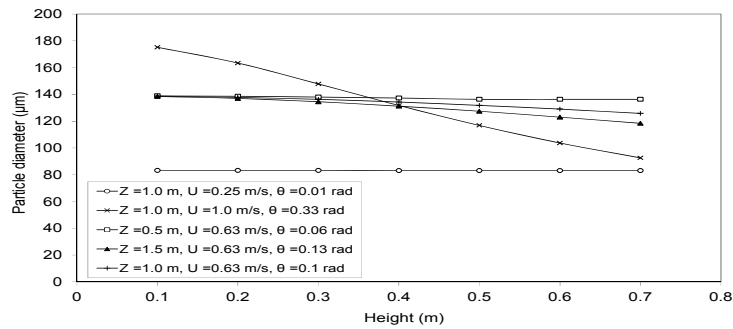

Figure 8. The influence of gas velocity and bed height on the design of the conical bed, a=0.75.

Figures 9 to 11 show particle size distribution as affected by balance factor (a) and height of the bed (Z) at three different gas inlet velocities (range: 0.41, 0.63 and 0.84 m s^{-1}). The angle of inclination, furthermore the particle distribution (PD) is poorly effected by the change in all variables, as shown in figure (9, and 10) for low gas inlet velocity 0.41 m/s and 0.63 m/s, which is prove the majority effect of the gas inlet velocity on the wall inclination and the PD. Figure 11 shows that at high inlet velocity (0.84 m s^{-1}), a bed height of 1.3 m provides a relatively more uniform particle distribution compared with the bed at a height of 0.7 m when the balance factor is 0.89. These results highlight the interaction effect between the three variables (U, Z, and a) considered in this analysis. The enhanced particle distribution achieved at the corresponding highest values of bed height and balance factor tested in this study is because an increase in 'a' leads to a reduction in the force needed to produce homogeneous fluidization of particles, and increased gas inlet velocity results in relatively higher forces exerted in the column, which improve particle distribution within the column.
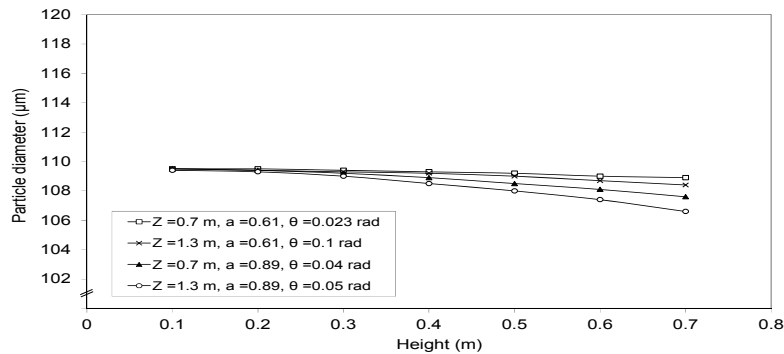

Figure 9. Particle size distribution as affected by balance factor (a) and height of the bed (Z) at gas inlet velocity 0.41 m/s.
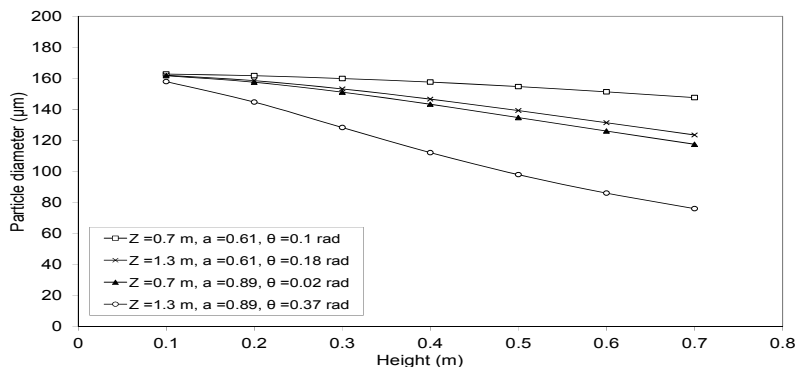
Figure 10. Particle size distribution as affected by balance factor (a) and height of the bed (Z) at gas inlet velocity 0.63 m/s.
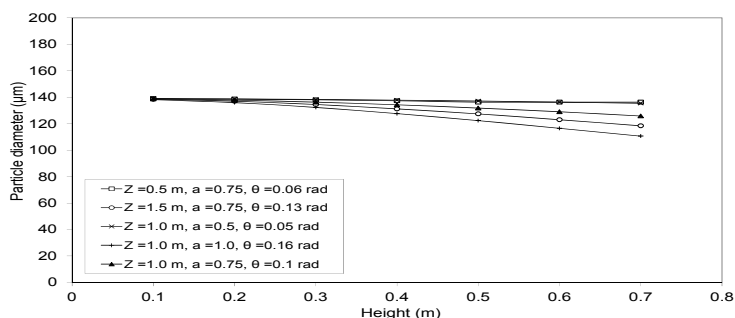

Figure 11. Particle size distribution as affected by balance factor (a) and height of the bed (Z) at gas inlet velocity 0.84 m/s.

Figure 12 shows the combined effects of the three variables (U, Z, and a) on the required inclination of the conical fluidized bed wall. When the balance factor is maintained at 0.75 and the gas inlet velocity is set at 0.63 m s^{-1}, there is a small increase in the required bed inclination with increasing bed height from 0.2 m to 1.5 m. However, a change in the balance factor (from a =0.2 to a =1.5) at a constant bed height of 1 m and constant gas inlet velocity of 0.63 m s^{-1}, show better effect on the inclination of the bed walls. The bed angle of inclination can be increased from around 0.0 rad to 0.3 rad. However, the angle of the bed wall is significantly more sensitive to changes in gas inlet velocity, as indicated by the response obtained for the wall angle of inclination (θ), when the balance factor is maintained at 0.75 and bed height at 1 m. The angle of the bed wall increase from around 0.0 rad at 0.23 m/s to 0.8 rad around 1.5 m/s gas velocity.
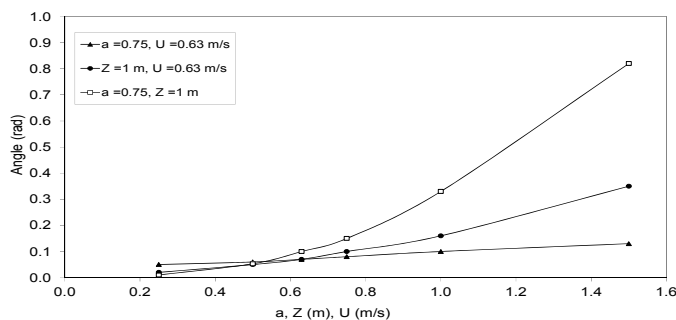

Figure 12. Determination of the angle of inclination (θ) as a function of the balance factor (a), height (Z) and velocity (U).

6. Summary

The arc shape of the distributor was selected and designed to distribute the inlet gas at the same inclination of the bed walls. This means that the gas inlet is introduced to the bed with an angle of inclination. The difference between a conical fluidized bed with flat and an arc shaped distributor is the elimination of dead zones. Dead zones happen in conical fluidized beds with flat distributors at the area where the gas does not reach (the zone out of the area of the distributor). The parameters selected in this research have direct impact on the performance of the fluidized bed with the arc shape distributor. Gas velocity and angle have impact on the drag force and bouncy force acting on the particles in

the bed. The angle of inclination of the bed walls is dependent on the arc shaped distributor. This angle cannot exceed a specific value due to gravity force. The balance factor (a) was introduced to balance between the vertical and horizontal forces exerted on the particles.

The main conclusions can be derived from this research is that design of homogenous conical fluidized bed is highly dependent on the design of the arc shape distributor. The angles of the holes in the distributor have to be at the same angle of the bed walls. Also, the thickness of the distributor is crucial in order to provide the inlet gas with sufficient energy to fluidize the particles in the bed. Theoretical, it is possible to create a homogeneous fluidization process using an arc shaped distributor. This can be applied in drying processes where the dried product can be collected from the top while drying in progress due to the difference in particles weights and fluidization velocities. The conical and arc shaped bed and distributor, respectively, can create layers of different fluidization velocities.

7. Nomenclature

Notation	Definition	Unit
a	Balance factor	---
A	Arc length of distributor	m
Ar	Archimedes number	---
D_d	Distributor diameter	m
D_i , D_o	Diameter of conical bed	m
d_{pi}	Particle diameter	m
d_v	Equivalent particle diameter	m
F	Force exerted on the particle	N
g	Gravity acceleration	$m\ s^{-2}$
K	Increment in column diameter	m
Q_o	Gas flow rate	$m^3\ s^{-1}$
R	Distributor diameter	m
r_o	Radius of bas	m
u_g	Gas velocity	$m\ s^{-1}$
U_i , U_o	Gas velocity, any position, and inlet	$m\ s^{-1}$
U_{mf}	Minimum fluidization velocity	$m\ s^{-1}$
V_p	Particle volume	m
x	Height of distributor at the middle point	m
Z	Height of bed	m
μ	Gas viscosity	$kg\ m^{-1}\ s^{-1}$
ρ_b	Bed density	$kg\ m^{-3}$
ρ_g	Gas density	$kg\ m^{-3}$
ρ_p	Particle density	$kg\ m^{-3}$
φ	Angle of the distributor with respect to x axis	rad
θ	Angle of the conic wall with respect to y axis	rad

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