Re-Estimating Inflation Threshold Level for Tanzania

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Abstract

The study seeks to estimate the relationship between inflation and economic growth, as well as the headline inflation threshold level beyond or below which Tanzania's economic growth is constrained. This was achieved through the Ordinary Least Squares (OLS) regressions employing quarterly data spanning the period 2001:1 to 2021:4. The findings suggest that the coefficient of inflation variable that captures the effect of low inflation on growth is statistically significant and positive, implying that low inflation is pro-growth. One percent increase in inflation leads to an economic growth of 0.352 percent. Furthermore, the coefficient of the high inflation proxy variable has a negative sign with the inflation threshold level being seven percent. At this level, the total effect of inflation on growth is estimated at 0.3494 percent. Moreover, optimal inflation levels of one to three percent have no impact on growth, as mirrored by invariable adjusted R^2 .

The recommendations from the results of this study are three-fold. First, the Bank of Tanzania may consider inflation targets below seven percent but above three percent in the monetary policy planning to continue supporting economic growth. Second, since the Bank has largely depended on inflation behaviour in informing inflation targets to choose, which ended into picking targets far from the optimal inflation, it is essential that the Bank also benefits from empirically estimated threshold rates. Third, in order to utilize any new information emanating from structural changes and developments in the economy, inflation threshold level should be re-estimated regularly.

Keywords: Tanzania, Inflation, Optimal inflation, Inflation and growth, Econometric analysis

1. Introduction

Globally, price stability has been the major goal of monetary policy. For many economic policy makers, the main interest has been to sustain high economic growth with stable price levels. High inflation is not desirable because it can negatively affect the economy by disrupting smooth functioning of markets, thus impeding efficient resource allocation; imposing welfare costs on the society; discouraging savings and investment; inhibiting financial development; and reducing international competitiveness (see, Ghosh and Phillips, 1998; Khan and Senhadji, 2001; Billi and Khan, 2008; Frimpong and Oteng-Abayie, 2010; Sindano, 2014; and Chindengwike, 2023). Businesses and households are more affected during times of high and unpredictable inflation (Barro, 1996).

It is not surprising therefore that countries seek to maintain low and stable inflation in their economies. According to Billi and Khan (2008), and Ghosh and Phillips (1998), inflation should not be allowed to fall below zero or be very low because of possible growth-harming effects.

How low should inflation be allowed to fall is an empirical issue, largely involving estimating the inflation threshold level for a country or a group of countries (Ghosh and Phillips, 1998; Mubarik, 2005; Burdekin et al., 2004; Lopez-Villavicencio and Mignon, 2011; Seleteng et al., 2013; and Thanh, 2015). Such estimations are likewise of paramount importance because there is a trade-off in maintaining policies that combat inflation and those that boost economic growth.

The case in point on the inflation-growth trade-off challenge is the phenomenon observed across the world since the first half of 2021, which was characterized by upward inflationary pressures¹ amidst slowing/low economic growth

¹ This is caused by supply disruptions emanating from COVID-19 impact and geopolitical tensions including the Russia-Ukraine war and the associated economic sanctions.

rates. As a result, many central banks are faced with the dilemma of scaling down or unwinding their accommodative monetary policies to contain inflation against pursuing expansionary monetary policy stance to spur recovery of the economies. The impact is much severe for imports dependent and developing countries such as Tanzania (World Bank, 2022) due to the high pass-through of foreign inflation² to the domestic economy.

The challenge facing many central banks globally also feature in Tanzania. The overriding questions have been two-fold. What is the relationship between inflation and growth? What inflation target, besides the prevailing level of 5.4 percent in 2022/23, could be chosen amid the rising commodity prices in the country such that the monetary policy actions remain supportive of growth? This study attempts to provide answers to these questions using the most current data set. The threshold rate is useful in guiding the decision on inflation target(s) to choose in the monetary policy formulation endeavour so as to continue supporting economic growth. This is much so as the Bank transits from using the reserve money (monetary aggregate) targeting framework to an interest-based one. Here, a single level or a range of inflation targets are needed in monetary policy programing framework.

In summary, the key research objectives are to determine the relationship between inflation and growth in Tanzania, and estimate the appropriate inflation threshold level that would allow monetary policy to continue supporting economic growth while containing inflation.

2. Tanzania's Policy Perspective on Inflation

2.1 Price Stability Policy and Targets

Prior to 1995, monetary policy was predominantly geared at supporting Tanzania's economic development goal (Mbowe, 2010). In support, the Bank of Tanzania (BOT) pursued multiple monetary policy objectives, achieved by employing the direct monetary policy instruments. That policy setting led to oversupply of money in the economy, which culminated into high inflation rates associated with low economic growth rates, particularly in most of the 1980s and first half of the1990s. To arrest the situation, three cornerstone Acts were passed in the first half of 1990s. The Banking and Financial Institutions Act was enacted in 1991 with a view to liberalizing the banking sector. This Act was trailed by the Foreign Exchange Act (1994), which opened the foreign exchange market to market forces, and the Bank of Tanzania Act (1995) that refocused the primary monetary policy objective to maintaining price stability, principally through the use of indirect policy instruments. Unique in the new setting is that, price stability is considered to be an important contributor to high and sustainable economic growth. Inflation-growth targets are accordingly pronounced in every National Annual Budget and Monetary Policy Statements, aimed at tracking the Government's broad development objectives.

Looking at historical numbers spanning from 2002/03 to 2022/23, one tends to believe that setting of inflation targets in the country has largely been informed by the inflation behaviour rather than empirical evidences on the optimal inflation relative to economic growth. It is clear from Figure 1 that during periods of low inflation, the targets were mostly set at 4-5 percent; this is during 2002/03 to 2008/09. Single digit inflation targets prevailed when inflation was more than 10 percent in 2011/12 to 2019/20. As inflation moderated, the targets were reduced to 3-5 percent in 2020/21 and 2021/22. Following demand and supply mismatch globally leading to increases in commodity prices³, the inflation target was relaxed to 5.4 percent for the financial year 2022/23. Establishing the inflation threshold could provide additional but useful information in determining the targets to pick in the interest-based framework⁴.

 $^{^2}$ Inflation in some of developed economies (some of whom are Tanzania's trade partners) exceeded targets, with those of UK and Euro zone for example hitting double digits in the second half of 2022.

³ The mismatch was largely contributed by the reoccurrence of COVID-19 pandemic in China, and the Ukraine-Russia war.

⁴ This is more transparent and forward looking relative to the reserve money monetary policy framework (Bank of Tanzania-BOT, 2016).



Figure 1. Actual Inflation Against Targets

Source: Authors' compilation from various Bank if Tanzania Monetary Policy Statements.

2.2 Relationship between Inflation and Real GDP Growth

Generally the study finds no clear pattern between inflation and growth can be traced over the study period (Figure 2)⁵. Some few inverse relationships are evident—though not one-to-one—during the periods of high inflation. The case in point are the times of the global financial crisis in 2007-2009 and the Euro debt crisis of 2011-2013, which negatively impacted the Tanzania's economy. Such unclear pattern between inflation and growth warrants further analysis including by the aid of descriptive statistics, correlation and causality tests. This issue is pursued in detail in the subsequent sections.





Source: Authors' construction using data from Tanzania National Bureau Statistics

⁵ See, Mbowe (2010), p.48; and BOT (2016), p.24 for more details on evolution of inflation in Tanzania and inflation-growth relationship, respectively.

3. Literature Review

3.1 Theoretical Literature

Theoretical conceptualization of output growth and inflation nexus dates back to Adam Smith's classical era. Here, growth was postulated to be supply side driven, with an implicit negative relationship between inflation and growth. Over time, other theoretical interplays also came in including structuralist, monetarist, and Keynesian views. While the former theory suggests that inflation positively influences output growth through capital accumulation (Mundell 1965 and Tobin 1965), the latter two theories see inflation as detrimental to growth as it may lower domestic and foreign savings, reduce efficiency of resource allocation, and deteriorate the balance of payments (Mallik and Chowdhury, 2001; Dornbusch et al., 1996; and Barro, 1996). The Keynesians, on their part, view the economy not moving directly to a higher inflation rate but rather follows a transitional path where it rises then falls (i.e., non-linear relationship), see Dornbusch et al. (1996). Such a diverse inflation-growth effect is also evident under the neo-classical construction where authors such as Tobin (1965), Stockman (1981), and Sidrauski (1967) postulate a positive, negative, and no effect relationships, respectively. The hypothesis of non-linearity suggests that adverse effects of inflation on economic growth is not universal; it appears only when inflation exceeds some turning point or threshold level below which inflation has a positive or non-significant impact on economic growth.

3.2 Rundown on Empirical Literature

The empirical literature in this area, i.e., inflation-growth relationship, is plentiful. Two estimation approaches are evident from the literature. The first approach is linear Ordinary Least Squares (OLS) where the inflation threshold is obtained by tracing the level of inflation that minimizes the Residual Sum of Squares (RSS) or maximizes the adjusted R^2 . The second is introduction in the OLS model a nonlinear inflation variable (i.e., a squared inflation variable) to capture the threshold effect.

On empirical results, while some of the studies argue for a negative relationship between inflation and output growth, others suggest a case for an optimal level (non-linearity) where inflation may be harmful to output growth. Studies which suggest existence of inflation optimal levels, which is the focus of the current study, are summarized in Table 1.

Authors	Country/Group	Results										
	Developed countries											
Balcilar, Gupta and Jooste	USA (1801 to 2013)	Growth and inflation relationship is hump shaped —that										
(2019)		higher levels of inflation reduce growth more compared to										
		low inflation or deflation. Inflation above 2% negatively										
		affects growth.										
Hwang and Wu (2011)	China (1986 to 2006)	Inflation threshold effect is highly significant and robust in										
		China. Above the 2.5% threshold, every 1 percentage point										
		increase in the inflation rate impedes economic growth by										
		0.61%; below this threshold, every 1 percentage point										
		increase in the inflation rate stimulates growth by 0.53%.										
Omay and Kan (2010)	Canada, France, Italy, Japan, UK	Inflation and growth are negatively related for the inflation										
	and USA	rates above the critical threshold level of 2.52%.										
Yerger and Freeman (2006)	Germany (1962 Q1 to 1998 Q4)	There is a discernible difference in the impact of inflation										
		upon productivity growth in Germany depending upon the										
		inflationary regime. In the low inflationary regime (below										
		2.95%) there is no statistically significant impact from an										
		inflation shock upon productivity, but in the high										
		inflationary regime the inflation shock has a significant										
		negative impact upon productivity growth.										
	Industrialized against non-in	dustrialized countries										
Kremer, Bick and Nautz	124 countries (1950 to 2004)	For industrialized countries inflation threshold of about 2%										
(2013)		is confirmed, whereas for non-industrialized countries,										
		inflation rates exceeding 17% are associated with lower										
		economic growth.										
	Developing and emerg	ging economies										
Komain (2017)	Thailand (1990 to 2015)	Inflation rate above 3% can jeopardize economic growth										
		rate.										
Mubarik (2005)	Pakistan (1973-2000)	The estimated model suggests 9 percent threshold level of										
		inflation above which inflation is inimical for economic										
		growth.										
Munir, Mansur and Furuoka	Malaysia (1970 to 2005)	The inflation threshold level is 3.89%. In addition, below the										
(2009)		threshold level, there is a statistically significant positive										
		relationship between inflation rate and growth.										
Sinelnikova-Muryleva and	Three country groups -the	Threshold above which a significant negative impact of										

Table 1. Summary of Empirical Results on Inflation Threshold Levels

Makeeva (2020)	largest emerging market countries (EM countries), EM countries with main source of earnings from export of raw materials, post-Soviet countries and central	inflation on Gross Domestic Product (GDP) growth rates a found at 4% for the largest EM and post-Soviet countrie 3.5% for EM countries exporters of raw materials and 5.5% for CEE countries.		
	and eastern Europe countries (CEE countries) (1990 to 2018)			
	African cour	ıtries		
Frimpong and Oteng-Abayie (2010)	Ghana (1960-2008)	Inflation threshold level of 11% at which inflation starts to significantly hurt economic growth		
Leshoro (2012)	South Africa (1980:Q2 to 2010:Q3)	Inflation threshold level occurs at 4%. At inflation levels below and up to 4%, there is a positive but insignificant relationship between inflation and growth. The relationship becomes negative and significant when the inflation rate is above 4%.		
Mosikari and Eita (2018)	Swaziland (1980 to 2015)	Inflation rate beyond optimal level of 12 percent decrease growth by 1.02 percent		
Salami and Kelikume (2010)	Nigeria (1970-2008)	The optimum inflation rate of 8% is found beyond which inflation is inimical to growth.		
Yabu and Kessy (2015)	Tanzania, Kenya and Uganda (1970 to 2013)	Average inflation beyond 8.46% has statistically significant and negative impact on economic growth for the three EAC partner states. For individual countries, optimal level of inflation for Kenya is 6.77%; Tanzania, 8.80%; and Uganda, 8.41%.		

Source: Authors' compilation from different sources.

As shown in Table 1, inflation threshold levels vary amongst industrialized and developing countries. Even in the group of developing and emerging market economies, countries with more developed economies exhibit lower inflation threshold levels for Thailand, Malaysia and South Africa). Developed economies experience low inflation threshold levels in the range of 2.0 to 2.95 percent, whereas for the developing and emerging economies, it is between 3.0 and 9.0 percent. In Africa, the threshold levels are within 4.0 and 12.0 percent, with South Africa exhibiting the lowest inflation threshold level of 4 percent.

Studies of this nature are scanty in Tanzania. Known to the authors, there is only one cross-country study by Yabu and Kessy (2015) that used annual data up to 2013 while introducing a squared inflation variable in the model. Since the Tanzanian economy has witnessed significant structural changes associated with increasing integration of the economy to that of the world, it is crucial to exploit the new information in determining the inflation beyond which growth is constrained. Goncalves and Salles (2008) and Lin and Ye (2009) underscore the need to utilize all available information in estimating inflation threshold levels, implying the levels could change with developments in an economy. Unlike Yabu and Kessy's study, the current one uses quarterly data, thus, capturing better the short-term dynamics in the economy. It also employs a different estimation approach (as illustrated in the methodology section) for robustness check purposes.

4. Estimation Approach

4.1 Model

In analysing threshold level of inflation in Tanzania, the model by Khan and Senhadji (2001) is adopted with some modification to suit Tanzanian environment. The model was used by Khan and Senhadji to analyse inflation threshold level for industrial and developing countries and it has been adopted by many other studies including developing and emerging market economies.

The model comprises four variables: the economic growth rate, inflation rate, population growth, and investment-GDP ratio. The latter two are control variables, considered in the model because they enhance growth (see, Solow, 1956; Mankiw et al., 1992; and Salai-i-Martin, 1997). Our conjecture is that inflation in Tanzania has an adverse effect on economic growth after it exceeds a certain limit.

The threshold model can be specified as follows:

$$rgdp_{t} = \alpha_{0} + \alpha_{1}\inf_{t} + \alpha_{2}D_{t}^{*}(\inf_{t} - k) + \alpha_{3}pop_{t} + \alpha_{4}inv_{t} + e_{t}, \qquad (1)$$

where, *t* is the time indicator; $rgdp_t$, the growth rate of real GDP; inf_b Consumer Price Index (CPI) inflation rate; *pop*, the growth rate of population, all variables are in log difference. The log transformation helps in smoothing time trend in the dataset (Mubarik, 2005) and provides best fit in the class of non-linear models (Khan and Senhadji, 2001). *invr*_t is the percentage ratio of private investment spending to GDP; *k*, threshold level of inflation; e_b the error term; a_0 , a

constant; and α_i (where, i=1...4) are coefficients. The relationship between inflation and growth is captured by α_1 . D_t is a dummy variable, in which:

$$D_t = 1: \inf_{k} > k, = 0: \inf_{k} \le k \text{ and } D_t = 0: \inf_{k} \le k$$
 (2)

The parameter *k* possesses the property that the relationship between inflation and growth is given by α_1 , representing low inflation rate; and high inflation rate represented by $\alpha_1 + \alpha_2$. If α_2 is statistically significant, the impact of inflation on economic growth will be added to see their impact on economic growth. That is, the effect of inflation on output growth is given by α_1 if the economy is faced by less or equal to threshold inflation, and $\alpha_1 + \alpha_2$ when the country experiences higher inflation rate.

Since the value of k is arbitrary, chosen in an ascending order (i.e., 1,2,3...), the optimal k can be obtained from estimates of equation (1) by selecting the value from estimated equation that minimizes the sum of squared residuals from the respective regressions. Said differently, the optimal threshold level is the one that maximizes the adjusted coefficient of determination (\mathbb{R}^2). At this level, inflation has a significant impact on growth (Mubarik, 2005 and Frimpong and Oteng-Abayie, 2010).

In the current study, the model is modified by adding more control variables to avoid growth model misspecification (equation 3). The explanatory variables are: percentage ratio of credit to GDP (*fin*) to capture the effect of finance in economic growth, degree of openness (*ope*) measured as percentage ratio of Tanzania's total external trade (exports and imports) to GDP. As Tanzania opens itself to the world, it benefits from capital flows (investment) and external market for the country's goods and services; these contribute to economic growth. With this modification, we end up with the following equation:

$$rgdp_{t} = \alpha_{0} + \alpha_{1}\inf_{t} + \alpha_{2}D_{t} * (\inf_{t} - k) + \alpha_{3}pop_{t} + \alpha_{4}inv_{t} + \alpha_{5}fin_{t} + \alpha_{6}ope_{t} + e_{t}.$$
 (3)

All coefficients in equation (3), except α_2 , are assumed to bear positive signs. For α_2 , the sign may be positive or negative.

4.2 Estimation Technique

Estimations of the baseline model is done using the Ordinary Least Squares (OLS) method. Since inflation could be non-exogenous in the growth-inflation model leading to biased estimated parameters (Khan and Senhadji, 2001), and that the effect could be felt with a lag, estimations are also carried out by Two-Stage Least Squares (2SLS) and with a lag.

The threshold level of inflation is computed for headline (overall) inflation, which is the Government's main reference variable for fiscal and monetary policy decisions. Price stability is perceived to be crucial for supporting high and sustainable growth of the economy.

4.3 Data Type and Sources

The ambition was to estimate the model using quarterly data, spanning the period 1995 ton2021, largely to capture the period when the country adopted price stability as its overriding monetary policy objective and to increase the degree of freedom. But, due to data limitations only quarterly data series from 2001:1 to 2021:4 were employed. Data related to consumer price index (used to compute inflation), population and real GDP were sourced from the Tanzania National Bureau of Statistics, while those of credit, investment and trade were obtained from BOT.

The actual credit (LOGFIN), investment (LOGINV) and openness (LOGOPE) variables were instead used in estimations to allow for log difference transformation. Despite the change, as depicted in appendix Figure A1, the two sets of variables are not qualitatively different (see RGDP scaled variables: LOGFIN_R, LOGINV_R and LOGOPE_R) suggesting either of them can be employed. CPI and RGDP were seasonally adjusted to remove seasonal components to allow for a meaningful comparison between observations. The inflation threshold variable was constructed using the actual inflation data while assuming an optimal inflation levels of 1 to 10. The graphs of the ultimately used variables are appended as Figure A2.

4.4 Pre estimation Tests

As pointed out earlier, macroeconomic data are characterized by a stochastic trend, which if unresolved, the statistical behaviour of the estimators will be influenced by such a trend such that results may be spurious. Hamilton (1994) suggests different methods of overcoming the problem of spurious regression arising from using non-stationary time series. These include using a lagged endogenous variable as an explanatory variable and differencing the non-stationary time series (until they become stationary) before variables are used in a regression. Another approach is to transform

variables into growth rates and ratios. This notwithstanding, tests on correlation and causality help to trace relationships among the variables. Discussions on pre-estimation tests is undertaken in detail below.

All variables (in logs) exhibit low standard deviation suggesting stability in the data generating process, (Table 2). As portrayed in Figure 3, the series display an upward trend. Generally, the variables are non-stationary in levels, but strongly stationary after the first difference with intercept and trend (see, Table 3 and Appendix Figure A2). With these results, the variables could be considered in log difference.

Table 2. Descriptive Statistics of Log Variables

	logrgdp	loghcpi	logfin	loginv	logope	logpop
Mean	16.73	4.06	15.46	14.10	15.38	16.19
Median	16.74	4.15	15.78	14.21	15.79	16.19
Maximum	17.36	4.66	16.92	15.13	16.50	16.50
Minimum	16.08	3.36	12.91	12.60	13.59	15.91
Std. Dev.	0.38	0.44	1.22	0.76	0.86	0.17
Skewness	-0.03	-0.20	-0.57	-0.56	-0.71	0.08
Kurtosis	1.81	1.52	2.03	2.06	2.13	1.82
Jarque-Bera	4.97	7.88	7.85	7.53	9.70	4.93
Probability	0.08	0.02	0.02	0.02	0.01	0.08
Sum	1405.07	325.10	1298.43	1184.32	1291.85	1360.08
Sum Sq. Dev.	12.25	15.05	123.42	47.97	61.84	2.47
Observations	84.00	80.00	84.00	84.00	84.00	84.00

Source: Authors' computations



Figure 3. Plots of Log Variables

Source: Authors' computations

		Augmented D	ickey-Fuller		Phillips-Perron				
Variable	Le	vel	1st Dif	ference	Le	vel	1st Difference		
variable		Intercept and		Intercept and		Intercept and		Intercept and	
	Intercept	trend	Intercept	trend	Intercept	trend	Intercept	trend	
logrgdp	-0.8929	-6.0150***	-9.5908***	-9.5911***	-0.3555	-6.1401***	-20.8429***	-22.9220***	
loghcpi	-1.3605	-0.3658	-4.2752***	-4.4807***	-1.1609	-0.2453	-4.2902***	-4.4835***	
logfin	-6.8404***	-0.2723	-1.9942	-8.6354***	-6.7945***	-0.1772	-5.7475***	-8.6880***	
loginv	-1.9467	0.2408	-2.0046	-3.7209**	-1.7385	0.1470	-1.7475	-2.1393	
logope	-2.6397*	-0.9606	-10.7905***	-11.3844***	-3.6045***	-1.5563	-9.2334***	-14.2040***	
logpop	1.4755	-1.9863	-3.3485**	-3.7203**	1.6131	-1.7619	-5.2572***	-5.5001	

Table 3. Unit Root Tests

Note: ***, **, and * means statistically significant at 1%, 5%, and 10%, respectively.

Source: Authors' computations

Furthermore, the explanatory variables appear to be positively and highly correlated with LOGRGDP, the dependent variable (Table 4). High correlation coefficients are also evident across explanatory variables, a tendency normally observed in macroeconomic variables. The high correlation coefficients among explanatory variables points to the need to also opt for lags of the variables or use the variables one at a time to avoid multicollinearity. The importance of using lags is also justified by causality tests, which are statistically significant, running from the dependent variable to some explanatory variables including LOGFIN and LOGPOP (see attached Table A1).

Table 4. Correlation Coefficients

Variable	logrgdp	loghcpi	logfin	loginv	logope	logpop
logrgdp	1	0.987	0.973	0.661	0.938	0.999
loghcpi	0.987	1	0.983	0.713	0.956	0.983
logfin	0.973	0.983	1	0.777	0.984	0.966
loginv	0.661	0.713	0.777	1	0.805	0.638
logope	0.938	0.956	0.984	0.805	1	0.927
logpop	0.999	0.983	0.966	0.638	0.927	1

Source: Authors' computations

5. Results and Discussions

Table 5 summarizes regression results tracing the threshold level of inflation beyond which growth is constrained. In the baseline OLS model, the coefficient of inflation variable, which captures the effect of low inflation on growth, is statistically significant and positive. An increase in inflation by 1 percent, for example, could stimulate growth by about 0.352 percent.

The coefficient reflecting the impact of high inflation on growth bears a negative sign with the inflation threshold level being seven percent. At this level of inflation, the requisite coefficient is statistically significant at one percent with the highest adjusted R^2 of 0.233. The total effect of inflation on growth is estimated at 0.3494 percent; indicating in aggregate inflation is pro-growth. Detailed results of the baseline OLS model are appended as Table A2⁶.

Picking an inflation threshold of eight percent for example would impose a burden on growth estimated at -0.0026 per unit compared to -0.0024 per unit likely to emanate from an optimal inflation level of seven percent. Although inflation threshold of six percent appears statistically significant when the regression accounts for a lag, such a level of inflation is associated with a lower adjusted R^2 of 0.2002, pointing to a possibility to accommodate a higher inflation target to spur growth.

 $^{^{6}}$ The F-test suggests that the model fits the data well, with F-statistic of 4.382 and p=value of 0.0004 which is far less than the 1 percent significance level. This fact is also supported by residuals plotted in appended Fig. A4, which exhibit a random walk (stability). Also, the Q-test (Figure. A5) does not provide any evidence to support presence of autocorrelation and partial correction in the data as the residuals fall within the estimated bounds.

Another key finding of this study is that, the optimal inflation levels of 1 to 3 percent do not have impact on growth, as reflected by unchanging adjusted R^2 . This infers that inflation targets in this range could safely be ignored.

In 2SLS regressions, the coefficient of inflation threshold variable is significant for the seven percent. But this has a relatively high standard error (S.E.) of regression⁷. Although the overall model for the six percent inflation threshold yields the lowest S.E. of regression, the coefficient thereof appears statistically insignificant.

Table 5. Inflation Threshold Results

Ordinary Least Squares, OLS					Two-stage Least Squares, 2SLS								
		No Lag			One Lag			No lag			One lag		
Threshold	dlogrgdp	Threshold variable		dlogrgdp	Threshold variable		dlogrgdp	Threshold variable	SEof	dlogrgdp	Threshold variable	SEof	
level	Coefficient; p-	Coefficient; p-	Adj R^2	Coefficient;	Coefficient;	Adj R^2	Coefficient;	Coefficient;	S.E. 01	Coefficient	Coefficient	S.E. 01	
	value in	value in		p-value in	p-value in		p-value in	p-value in	regression	; p-value	; p-value	regression	
	brackets	brackets		brackets	brackets		brackets	brackets		in brackets	in brackets		
k0	-0.077436		0.146794	0.025816		0.131381	1.905586		0.192173	0.025816		0.013132	
	(0.6035)			(0.8622)			(0.9731)			(0.8622)			
k1	0.260841	-0.00132	0.181314	0.384509	-0.001278	0.149507	0.931137	-0.001674	0.014969	0.306337	-0.000999	0.013005	
	(0.2449)	(0.0483)**		0.1583	0.1174		(0.8346)	(0.3094)		(0.3567)	(0.3462)		
k2	0.260841	-0.00132	0.181314	0.384509	-0.001278	0.149507	0.931137	-0.001674	0.014969	0.306337	-0.000999	0.013005	
	(0.2449)	(0.0483)**		0.1583	0.1174		(0.8346)	(0.3094)		(0.3567)	(0.3462)		
k3	0.260841	-0.00132	0.181314	0.384509	-0.001278	0.149507	0.931137	-0.001674	0.014969	0.306337	-0.000999	0.013005	
	(0.2449)	(0.0483)		0.1583	0.1174		(0.8346)	(0.3094)		(0.3567)	(0.3462)		
k4	0.279399	-0.001429	0.187227	0.419415	-0.001437	0.155822	0.711944	-0.001805	0.030417	0.331297	-0.001115	0.01296	
	0.21	(0.0357)**		0.1226	(0.0848)*		(0.924)	(0.6074)		(0.3219)	(0.309)		
k5	0.308811	-0.001672	0.201823	0.491116	-0.001798	0.171939	0.568572	-0.001875	0.043567	0.388766	-0.001403	0.012842	
	(0.1527)	(0.0171)**		(0.0663)*	(0.0379)**		(0.9424)	(0.8004)		(0.2396)	(0.2211)		
k6	0.362587	-0.002134	0.229567	0.58228	-0.002383	0.200216	0.475974	-0.002429	0.064531	0.471537	-0.001909	0.012626	
	(0.0814)*	(0.0042)***		(0.0241)**	(0.0095)***		(0.972)	(0.8188)		(0.1421)	(0.1209)		
k7	0.352684	-0.002414	0.232825	0.551697	-0.002576	0.194926	0.04614	-0.003158	0.120323	0.496221	-0.002305	0.012649	
	(0.0829)*	(0.0036)***		(0.0303)**	(0.0123)**		(0.9988)	(0.8479)		(0.1192)	(0.0978)*		
k8	0.314513	-0.002628	0.226856	0.46815	-0.002544	0.177613	2.954315	0.002136	0.367217	0.526233	-0.002878	0.012786	
	(0.1117)	(0.0049)***		(0.06)*	(0.0287)**		(0.9808)	0.9962		'(0.0953)*	(0.0739)*		

Source: Authors' computations.

The findings in this study compare well with those found in countries with similar economies, where developing economies exhibit relatively high inflation threshold levels. Such a situation could be explained by the fact that the economies are operating far below their potentials so that increases in prices are crucial in spurring growth, chiefly from the supply-side. As the economy advances, the required threshold level declines as well. This phenomenon could be operating in Tanzania's economy as well. Certainly, the seven percent threshold found in this study is below 8.80 percent obtained by Yabu and Kessy (2015), probably reflecting economic advancements, which also helped the country graduate to lower middle income group in 2020. Worth noting as well is the fact that Tanzania is catching up with Kenya, the more advanced economy in the region, that was found to exhibit an inflation threshold of around 6.77 percent in that study.

It is worthy pointing that, in the whole study period, it is only 2008/09 when inflation target in Tanzania coincides with the estimated seven percent inflation threshold. As indicated earlier, most of the time inflation targets were far below or above the threshold level, suggesting possibility for improvement.

6. Conclusion and Policy Recommendations

Price stability is an important policy drive for many countries, mostly pursued with a view to stimulating and sustaining high economic growth. In order to attain this, countries target to attain low and stable inflation. Due to costs associated with high inflation on growth, understanding the inflation threshold rate beyond which growth is hampered is stressed. This study attempts to contribute to this using the OLS regression technique and Tanzanian quarterly data spanning the period 2002:1 to 2021:4. Two research questions are addressed: What is the relationship between inflation and growth? What inflation target, besides the prevailing 5.4 percent, could be chosen amid the rising commodity prices in the country such that the monetary policy actions continue to spur growth?

⁷ S.E. of regression is used to identify the optimal inflation level because in 2SLS, adjusted R^2 is not meaningful and may bear a negative value since some of the regressors enter the model as instruments when the parameters are estimated. Here, the model's residuals are computed over a set of regressors different from those used to fit the model, while the residual sum of squares (RSS) are not constraining to be smaller than the total sum of squares (TSS) leading to negative R^2 .

The findings suggest that the coefficient of inflation variable is statistically significant and positive—indicating low inflation supports growth—in which a one percent increase in inflation would lead to an increase in growth by 0.352 percent. The inflation threshold level is seven percent. At this level, the total effect of inflation on growth is estimated at 0.3494 percent suggesting, overall, inflation in the country is pro-growth. Choosing an inflation threshold of eight percent for example would inflict a burden on growth of around -0.0026 per unit compared to -0.0024 per unit likely to originate from the optimal inflation level of seven percent.

It is also found that the optimal inflation levels of 1 to 3 percent have no impact on growth, as echoed by invariable adjusted R^2 .

It is recommended that the Bank may consider inflation targets below seven percent but above three percent in its monetary policy planning with a view to stimulating growth in the country. Since the Bank has largely depended on inflation behaviour in informing inflation targets to choose, which culminated in setting targets far below the optimal inflation, it is recommended to as well benefit from empirically estimated optimal targets. This would reduce the possibility to hamper price increases in the economy, consequently limiting supply. The inflation threshold level should be re-estimated regularly to benefit from any new information stemming from structural changes and advancements in the economy.

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Authors contributions

Dr, Wilfred Mbowe was responsible for study design, econometric estimations and revising. Ms Hossana Mpango was responsible for data collection, reviewing the policy & regulatory environment and literature, and formatting of tables and charts. All authors read and approved the final manuscript. In aggregate, both authors contributed equally to the study.

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The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Obtained.

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The data that support the findings of this study are available on request from the corresponding author. The data are not publicly available due to privacy or ethical restrictions.

Data sharing statement

No additional data are available.

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Appendices



Figure A1. Plots of FIN, INV, OPE as Ratios of RGDP against Logs of Actual Variables Source: Authors' computations

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Source: Authors' computations

Figure A3. Inflation Threshold Levels used in Regression

Note: SER denotes an inflation threshold level. Source: Authors' computation.

Table A1. Granger Causality Tests

Pairwise Granger Causality Tests			
Date: 12/25/22 Time: 08:00			
Sample: 2001Q1 2021Q4			
Lags: 2			
Null Hypothesis:	Obs	F-Statistic	Prob.
LOGHCPI does not Granger Cause LOGRGDP	78	0.51359	0.6005
LOGRGDP does not Granger Cause LOGHCPI		2.16005	0.1226
LOGFIN does not Granger Cause LOGRGDP	82	0.49751	0.6100
LOGRGDP does not Granger Cause LOGFIN		2.5518	0.0845*
LOGINV does not Granger Cause LOGRGDP	82	0.00536	0.9947
LOGRGDP does not Granger Cause LOGINV		1.44397	0.2423
LOGOPE does not Granger Cause LOGRGDP	82	0.13065	0.8777
LOGRGDP does not Granger Cause LOGOPE		0.84874	0.4319
LOGPOP does not Granger Cause LOGRGDP	82	1.76204	0.1785
LOGRGDP does not Granger Cause LOGPOP		5.45624	0.0061***
LOGFIN does not Granger Cause LOGHCPI	78	6.92308	0.0018***
LOGHCPI does not Granger Cause LOGFIN		0.24025	0.7871
LOGINV does not Granger Cause LOGHCPI	78	4.3725	0.0161**
LOGHCPI does not Granger Cause LOGINV		2.89935	0.0614**
LOGOPE does not Granger Cause LOGHCPI	78	6.82156	0.0019***
LOGHCPI does not Granger Cause LOGOPE		0.92899	0.3996
LOGPOP does not Granger Cause LOGHCPI	78	0.01448	0.9856
LOGHCPI does not Granger Cause LOGPOP		4.40844	0.0156**
LOGINV does not Granger Cause LOGFIN	82	0.47168	0.6257
LOGFIN does not Granger Cause LOGINV		3.09138	0.0511*
LOGOPE does not Granger Cause LOGFIN	82	3.93211	0.0237**
LOGFIN does not Granger Cause LOGOPE		4.16234	0.0192**
LOGPOP does not Granger Cause LOGFIN	82	0.69368	0.5028
LOGFIN does not Granger Cause LOGPOP		0.35285	0.7038
LOGOPE does not Granger Cause LOGINV	82	5.97178	0.0039***
LOGINV does not Granger Cause LOGOPE		1.64188	0.2003
LOGPOP does not Granger Cause LOGINV	82	0.1918	0.8259
LOGINV does not Granger Cause LOGPOP		0.01131	0.9888
LOGPOP does not Granger Cause LOGOPE	82	0.98958	0.3764
LOGOPE does not Granger Cause LOGPOP		0.2979	0.7432

Source: Authors' computations.

Dependent Variable: I	DLOGRGDP				Dependent Variable: D	LOGRGDP			
Method: Least Square	s				Method: Least Squares				
Date: 12/26/22 Time	e: 08:02				Date: 12/26/22 Time:	08:57			
Sample (adjusted): 20	02Q2 2021Q4				Sample (adjusted): 200	2Q3 2021Q4			
Included observations	: 79 after adjustn	ients			Included observations:	78 after adjustr	nents		
No lag					One lag				
Variable	Coefficient	Std. Error	t-Statistic	Prob.	Variable	Coefficient	Std. Error	t-Statistic	Prob.
С	0.035781	0.006716	5.32755	0	С	0.021886	0.007234	3.025491	0.0035
DLOGRGDP(-1)	-0.380225	0.100996	-3.764761	0.0003	DLOGRGDP(-1)	-0.543983	0.113121	-4.808848	0
DLOGHCPI	0.352684	0.200496	1.759056	0.0829	DLOGHCPI(-1)	0.58228	0.25251	2.305971	0.0241
DLOGFIN	-0.036136	0.041876	-0.862924	0.3911	DLOGFIN(-1)	-0.028338	0.042393	-0.668462	0.506
DLOGINV	0.007267	0.009237	0.786727	0.4341	DLOGINV(-1)	0.005411	0.010436	0.518505	0.6057
DLOGOPE	0.012857	0.01416	0.907987	0.367	DLOGOPE(-1)	0.00544	0.014569	0.373387	0.71
DLOGPOP	-2.167929	0.791328	-2.739608	0.0078	DLOGPOP(-1)	-0.318316	0.806747	-0.394567	0.6944
Threshold level: k=7	-0.002414	0.000801	-3.012318	0.0036	Threshold level: k=6	-0.002383	0.000894	-2.6666	0.0095
R-squared	0.301674	Mean depend	lent var	0.015562	R-squared	0.272924	Mean depe	ndent var	0.015509
Adjusted R-squared	0.232825	S.D. depende	ent var	0.014007	Adjusted R-squared	0.200216	S.D. depen	dent var	0.01409
S.E. of regression	0.012269	Akaike info	criterion	-5.867745	S.E. of regression	0.012601	Akaike info	o criterion	-5.813164
Sum squared resid	0.010687	Schwarz crit	erion	-5.627801	Sum squared resid	0.011115	Schwarz cr	iterion	-5.571451
Log likelihood	239.7759	Hannan-Qui	nn criter.	-5.771616	Log likelihood	234.7134	Hannan-Qu	inn criter.	-5.716402
F-statistic	4.381667	Durbin-Wats	son stat	2.269726	F-statistic	3.753721	Durbin-Wa	atson stat	2.159097
Prob(F-statistic)	0.000435				Prob(F-statistic)	0.001652			

Table A2: Inflation Threshold Level Results (OLS)

Source: Authors computations.

Figure A4. Actual-Fitted Residuals

Source: Authors' computations

Q-statistic probabilities adjusted for 1 dynamic regressor
Sample (adjusted): 2002Q2 2021Q4
Date: 12/28/22 Time: 09:25

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
	I I	1	-0.142	-0.142	1.6615	0.197
· ·	I III I	2	-0.222	-0.247	5.7417	0.057
	I 🛛 I	3	0.000	-0.081	5.7417	0.125
I 🔲 I	I I I	4	-0.081	-0.165	6.3079	0.177
i 📮 i	ן ום ד	5	0.119	0.060	7.5266	0.184
۱ Щ ۱	I I I	6	-0.131	-0.177	9.0388	0.171
I 🛛 I	I I I I	7	-0.020	-0.042	9.0757	0.247
1 1	I I I I	8	-0.006	-0.119	9.0786	0.336
· 🗩		9	0.207	0.213	13.011	0.162
I 🔲 I	I I I I	10	-0.091	-0.120	13.783	0.183
т Щ т	I I	11	-0.088	0.028	14.506	0.206
I 📮 I		12	0.095	0.003	15.371	0.222
i 🛄 i	l 🔲 i	13	0.080	0.182	15.990	0.250
i 🛯 i	I I I I	14	-0.049	-0.095	16.229	0.300
I 🛄 I		15	-0.143	-0.011	18.264	0.249
i 🛛 i	I I I I	16	-0.042	-0.151	18.442	0.299
r 🛄 r	l i 🎫	17	0.156	0.180	20.969	0.228
r 🔲 r	I I	18	0.133	0.028	22.824	0.197
· •	I I I I	19	-0.200	-0.035	27.101	0.102
i 🖡 i	I I	20	0.040	0.025	27.275	0.128
т р т		21	0.027	0.011	27.355	0.159
т ј т	1 1	22	0.029	0.001	27.452	0.195
т ц т		23	-0.028	-0.011	27.539	0.234
I 🔲 I	1 1 1	24	-0.138	-0.066	29.760	0.193
i 🛄 i	I ⊫ I	25	0.145	0.100	32.265	0.150
i 🏼 i	I I I I	26	0.061	0.011	32.712	0.171
1 🗓 1		27	-0.047	-0.012	32.985	0.198
I 🔲 I	I I I I	28	-0.171	-0.125	36.667	0.126
I 🖡 I	I 🛛 I	29	-0.013	-0.080	36.690	0.154
r 🗖 r	I I I I	30	0.117	-0.058	38.476	0.138
i 🛯 i	1 1	31	-0.057	-0.089	38.906	0.156
· 🛛 ·		32	-0.063	-0.085	39.438	0.172

*Probabilities may not be valid for this equation specification.

Figure A5. Correlogram – Q-Test

Source: Authors' computations.